

Hexaaquacadmium(II) 2,2'-(azino-dimethylidyne)dibenzenesulfonate dihydrate

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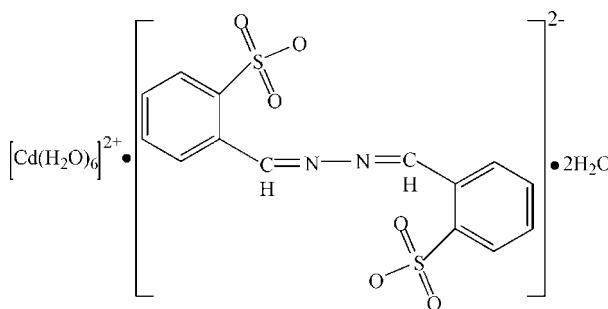
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Key indicators: single-crystal X-ray study; $T = 298\text{ K}$; mean $\sigma(\text{C}-\text{C}) = 0.003\text{ \AA}$; R factor = 0.023; wR factor = 0.061; data-to-parameter ratio = 13.4.

In the title compound, $[\text{Cd}(\text{H}_2\text{O})_6](\text{C}_{14}\text{H}_{10}\text{O}_6\text{N}_2\text{S}_2)\cdot 2\text{H}_2\text{O}$, the complete cation and anion are each generated by crystallographic inversion symmetry. In the crystal structure, the components form a three-dimensional network by way of $\text{O}-\text{H}\cdots\text{O}$ and $\text{O}-\text{H}\cdots\text{N}$ hydrogen bonds.

Related literature

For background to the properties and potential applications of organic-inorganic hybrid materials, see: Hagrman *et al.* (1998); Ranford *et al.* (1998).



Experimental

Crystal data

$[\text{Cd}(\text{H}_2\text{O})_6](\text{C}_{14}\text{H}_{10}\text{O}_6\text{N}_2\text{S}_2)\cdot 2\text{H}_2\text{O}$

$M_r = 622.89$

Triclinic, $P\bar{1}$

$a = 7.8329 (11)\text{ \AA}$

$b = 7.9824 (12)\text{ \AA}$

$c = 10.1010 (15)\text{ \AA}$

$\alpha = 92.723 (1)^{\circ}$

$\beta = 102.076 (2)^{\circ}$

$\gamma = 105.924 (2)^{\circ}$

$V = 590.19 (15)\text{ \AA}^3$

$Z = 1$

Mo $K\alpha$ radiation

$\mu = 1.17\text{ mm}^{-1}$

$T = 298 (2)\text{ K}$

$0.45 \times 0.40 \times 0.28\text{ mm}$

Data collection

Bruker SMART CCD diffractometer

Absorption correction: multi-scan (*SADABS*; Bruker, 2000)

$T_{\min} = 0.621$, $T_{\max} = 0.735$

3081 measured reflections
2041 independent reflections
1929 reflections with $I > 2\sigma(I)$
 $R_{\text{int}} = 0.018$

Refinement

$R[F^2 > 2\sigma(F^2)] = 0.023$

$wR(F^2) = 0.061$

$S = 1.06$

2041 reflections

152 parameters
H-atom parameters constrained
 $\Delta\rho_{\text{max}} = 0.33\text{ e \AA}^{-3}$
 $\Delta\rho_{\text{min}} = -0.42\text{ e \AA}^{-3}$

Table 1
Selected bond lengths (\AA).

| | | | |
|--------|-------------|--------|-------------|
| Cd1—O5 | 2.2555 (18) | Cd1—O6 | 2.2947 (18) |
| Cd1—O4 | 2.2589 (17) | | |

Table 2
Hydrogen-bond geometry (\AA , $^{\circ}$).

| $D-\text{H}\cdots A$ | $D-\text{H}$ | $\text{H}\cdots A$ | $D\cdots A$ | $D-\text{H}\cdots A$ |
|-----------------------------------|--------------|--------------------|-------------|----------------------|
| O4—H4A \cdots O2 ⁱ | 0.85 | 1.94 | 2.783 (3) | 171 |
| O4—H4B \cdots O1 ⁱⁱ | 0.85 | 2.03 | 2.872 (2) | 174 |
| O5—H5A \cdots O1 ⁱⁱⁱ | 0.85 | 1.99 | 2.831 (3) | 173 |
| O5—H5B \cdots O7 ^{iv} | 0.85 | 2.00 | 2.843 (3) | 173 |
| O6—H6A \cdots O7 | 0.85 | 2.08 | 2.881 (3) | 157 |
| O6—H6B \cdots N1 ^v | 0.85 | 2.15 | 2.993 (3) | 169 |
| O7—H7A \cdots O3 ^{vi} | 0.85 | 1.85 | 2.692 (3) | 172 |
| O7—H7B \cdots O2 ⁱⁱⁱ | 0.85 | 2.21 | 3.002 (3) | 156 |

Symmetry codes: (i) $x - 1, y - 1, z$; (ii) $-x + 1, -y + 1, -z + 1$; (iii) $-x + 2, -y + 1, -z + 1$; (iv) $-x + 1, -y, -z + 1$; (v) $-x + 1, -y + 1, -z$; (vi) $x, y - 1, z$.

Data collection: *SMART* (Bruker, 2000); cell refinement: *SAINT* (Bruker, 2000); data reduction: *SAINT*; program(s) used to solve structure: *SHELXS97* (Sheldrick, 2008); program(s) used to refine structure: *SHELXL97* (Sheldrick, 2008); molecular graphics: *SHELXTL* (Sheldrick, 2008); software used to prepare material for publication: *SHELXTL*.

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Supplementary data and figures for this paper are available from the IUCr electronic archives (Reference: HB2858).

References

- Bruker (2000). *SMART*, *SAINT* and *SADABS*. Bruker AXS Inc., Madison, Wisconsin, USA.
- Hagrman, D., Hammond, R. P. & Haushalter, R. (1998). *Chem. Mater.* **10**, 2091–2096.
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supplementary materials

Acta Cryst. (2008). E64, m1625 [doi:10.1107/S1600536808039032]

Hexaaquacadmium(II) 2,2'-(azinodimethylidyne)dibenzenesulfonate dihydrate

L.-C. Du

Comment

The design and synthesis of organic/inorganic hybrid materials have attracted intense attention in recent years owing to their potential practical applications, such as antitumor, antidiabetic, antitubercular activities, magnetism and catalysis [Ranford, *et al.*, 1998; Hagrman, *et al.*, 1998]. As part of our studies in this area, we now report the synthesis and crystal structure of the title compound, (I).

The Cd(II) centre is six-coordinate with six O donors of H_2O , and adopts distorted octahedral coordination (Table 1, Fig. 1). In the crystal, the molecules form a three-dimensional network by way of $\text{O}—\text{H}\cdots\text{O}$ and $\text{O}—\text{H}\cdots\text{N}$ hydrogen bonds (Table 2).

Experimental

A solution of 1.0 mmol 2-formyl-benzenesulfonic acid-hydrazine and 1.0 mmol NaOH in 5 ml 95% ethanol was added to a solution of 0.5 mmol $\text{Cd}(\text{CH}_3\text{COO})_2 \cdot 4\text{H}_2\text{O}$ in 5 ml ethanol at room temperature. The mixture was refluxed for 4 h with stirring, then the resulting precipitate was filtered, washed, and dried *in vacuo* over P_4O_{10} for 48 h. Colourless blocks of (I) were obtained by slowly evaporating from methanol at room temperature.

Refinement

H atom treatment??

Figures

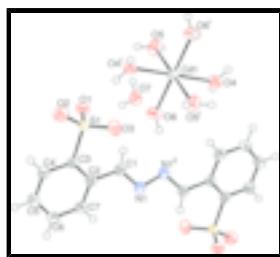


Fig. 1. The molecular structure of (I) showing 50% displacement ellipsoids for the non-hydrogen atoms. Symmetry codes: (i) $1-x, 1-y, 1-z$; (ii) $1-x, 1-y, -z$.

Hexaaquacadmium(II) 2,2'-(azinodimethylidyne)dibenzenesulfonate dihydrate

Crystal data

$[\text{Cd}(\text{H}_2\text{O})_6](\text{C}_{14}\text{H}_{10}\text{O}_6\text{N}_2\text{S}_2) \cdot 2\text{H}_2\text{O}$

$M_r = 622.89$

$Z = 1$

$F_{000} = 316$

supplementary materials

| | |
|---------------------------------|---|
| Triclinic, $P\bar{1}$ | $D_x = 1.753 \text{ Mg m}^{-3}$ |
| Hall symbol: -P 1 | Mo $K\alpha$ radiation |
| $a = 7.8329 (11) \text{ \AA}$ | $\lambda = 0.71073 \text{ \AA}$ |
| $b = 7.9824 (12) \text{ \AA}$ | Cell parameters from 2719 reflections |
| $c = 10.1010 (15) \text{ \AA}$ | $\theta = 2.7\text{--}28.3^\circ$ |
| $\alpha = 92.723 (1)^\circ$ | $\mu = 1.17 \text{ mm}^{-1}$ |
| $\beta = 102.076 (2)^\circ$ | $T = 298 (2) \text{ K}$ |
| $\gamma = 105.924 (2)^\circ$ | Block, colourless |
| $V = 590.19 (15) \text{ \AA}^3$ | $0.45 \times 0.40 \times 0.28 \text{ mm}$ |

Data collection

| | |
|--|--|
| Bruker SMART CCD diffractometer | 2041 independent reflections |
| Radiation source: fine-focus sealed tube | 1929 reflections with $I > 2\sigma(I)$ |
| Monochromator: graphite | $R_{\text{int}} = 0.018$ |
| $T = 298(2) \text{ K}$ | $\theta_{\text{max}} = 25.0^\circ$ |
| ω scans | $\theta_{\text{min}} = 2.1^\circ$ |
| Absorption correction: multi-scan (SADABS; Bruker, 2000) | $h = -9 \rightarrow 9$ |
| $T_{\text{min}} = 0.621$, $T_{\text{max}} = 0.735$ | $k = -5 \rightarrow 9$ |
| 3081 measured reflections | $l = -11 \rightarrow 12$ |

Refinement

| | |
|--|--|
| Refinement on F^2 | Hydrogen site location: inferred from neighbouring sites |
| Least-squares matrix: full | H-atom parameters constrained |
| $R[F^2 > 2\sigma(F^2)] = 0.023$ | $w = 1/[\sigma^2(F_o^2) + (0.0313P)^2 + 0.2007P]$ where $P = (F_o^2 + 2F_c^2)/3$ |
| $wR(F^2) = 0.061$ | $(\Delta/\sigma)_{\text{max}} = 0.001$ |
| $S = 1.06$ | $\Delta\rho_{\text{max}} = 0.33 \text{ e \AA}^{-3}$ |
| 2041 reflections | $\Delta\rho_{\text{min}} = -0.42 \text{ e \AA}^{-3}$ |
| 152 parameters | Extinction correction: SHELXL97 (Sheldrick, 2008), $F_c^* = kF_c[1 + 0.001xF_c^2\lambda^3/\sin(2\theta)]^{1/4}$ |
| Primary atom site location: structure-invariant direct methods | Extinction coefficient: 0.067 (3) |
| Secondary atom site location: difference Fourier map | |

Special details

Geometry. All e.s.d.'s (except the e.s.d. in the dihedral angle between two l.s. planes) are estimated using the full covariance matrix. The cell e.s.d.'s are taken into account individually in the estimation of e.s.d.'s in distances, angles and torsion angles; correlations between e.s.d.'s in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell e.s.d.'s is used for estimating e.s.d.'s involving l.s. planes.

Refinement. Refinement of F^2 against ALL reflections. The weighted R -factor wR and goodness of fit S are based on F^2 , conventional R -factors R are based on F , with F set to zero for negative F^2 . The threshold expression of $F^2 > \sigma(F^2)$ is used only for calculating R -factors(gt) etc. and is not relevant to the choice of reflections for refinement. R -factors based on F^2 are statistically about twice as large as those based on F , and R -factors based on ALL data will be even larger.

Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters (\AA^2)

| | <i>x</i> | <i>y</i> | <i>z</i> | $U_{\text{iso}}^*/U_{\text{eq}}$ |
|-----|-------------|-------------|--------------|----------------------------------|
| Cd1 | 0.5000 | 0.5000 | 0.5000 | 0.02922 (13) |
| N1 | 0.5732 (3) | 0.5473 (3) | -0.0282 (2) | 0.0336 (5) |
| O1 | 1.0298 (2) | 0.6986 (2) | 0.35433 (17) | 0.0384 (4) |
| O2 | 1.1817 (3) | 1.0036 (3) | 0.35043 (19) | 0.0465 (5) |
| O3 | 0.8508 (3) | 0.8917 (3) | 0.2790 (2) | 0.0477 (5) |
| O4 | 0.2044 (2) | 0.3385 (2) | 0.45818 (18) | 0.0406 (4) |
| H4A | 0.1847 | 0.2342 | 0.4229 | 0.049* |
| H4B | 0.1378 | 0.3362 | 0.5150 | 0.049* |
| O5 | 0.6085 (3) | 0.3128 (3) | 0.6297 (2) | 0.0471 (5) |
| H5A | 0.7201 | 0.3195 | 0.6358 | 0.057* |
| H5B | 0.5490 | 0.2060 | 0.6283 | 0.057* |
| O6 | 0.5347 (3) | 0.3561 (3) | 0.30977 (19) | 0.0448 (5) |
| H6A | 0.5293 | 0.2485 | 0.3123 | 0.054* |
| H6B | 0.4908 | 0.3730 | 0.2289 | 0.054* |
| O7 | 0.6167 (3) | 0.0337 (3) | 0.3703 (2) | 0.0468 (5) |
| H7A | 0.6908 | -0.0043 | 0.3358 | 0.056* |
| H7B | 0.6594 | 0.0466 | 0.4560 | 0.056* |
| S1 | 1.02370 (7) | 0.85670 (8) | 0.28844 (6) | 0.02847 (16) |
| C1 | 0.7223 (3) | 0.5998 (3) | 0.0615 (2) | 0.0303 (5) |
| H1 | 0.7234 | 0.5806 | 0.1517 | 0.036* |
| C2 | 0.8948 (3) | 0.6913 (3) | 0.0237 (2) | 0.0265 (5) |
| C3 | 1.0408 (3) | 0.8087 (3) | 0.1183 (2) | 0.0258 (5) |
| C4 | 1.2027 (3) | 0.8863 (3) | 0.0822 (3) | 0.0348 (6) |
| H4 | 1.2984 | 0.9650 | 0.1451 | 0.042* |
| C5 | 1.2224 (4) | 0.8469 (4) | -0.0476 (3) | 0.0423 (6) |
| H5 | 1.3316 | 0.8989 | -0.0717 | 0.051* |
| C6 | 1.0809 (3) | 0.7311 (4) | -0.1414 (3) | 0.0386 (6) |
| H6 | 1.0948 | 0.7044 | -0.2284 | 0.046* |
| C7 | 0.9177 (3) | 0.6542 (3) | -0.1061 (2) | 0.0337 (5) |
| H7 | 0.8223 | 0.5768 | -0.1701 | 0.040* |

Atomic displacement parameters (\AA^2)

| | U^{11} | U^{22} | U^{33} | U^{12} | U^{13} | U^{23} |
|-----|--------------|--------------|--------------|--------------|--------------|--------------|
| Cd1 | 0.03192 (17) | 0.02725 (17) | 0.02920 (17) | 0.01001 (10) | 0.00609 (10) | 0.00611 (10) |
| N1 | 0.0251 (10) | 0.0408 (12) | 0.0293 (11) | 0.0001 (9) | 0.0060 (8) | 0.0066 (9) |
| O1 | 0.0449 (10) | 0.0429 (10) | 0.0318 (9) | 0.0163 (8) | 0.0123 (8) | 0.0108 (8) |
| O2 | 0.0477 (11) | 0.0433 (11) | 0.0375 (10) | -0.0004 (9) | 0.0074 (8) | -0.0093 (9) |
| O3 | 0.0429 (10) | 0.0629 (13) | 0.0486 (12) | 0.0291 (10) | 0.0168 (9) | 0.0054 (10) |

supplementary materials

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|----|-------------|-------------|-------------|-------------|-------------|-------------|
| O4 | 0.0398 (10) | 0.0394 (10) | 0.0389 (10) | 0.0022 (8) | 0.0151 (8) | 0.0000 (8) |
| O5 | 0.0416 (10) | 0.0394 (11) | 0.0614 (13) | 0.0147 (9) | 0.0069 (9) | 0.0211 (9) |
| O6 | 0.0639 (12) | 0.0415 (11) | 0.0329 (10) | 0.0200 (10) | 0.0132 (9) | 0.0038 (8) |
| O7 | 0.0447 (11) | 0.0518 (12) | 0.0501 (12) | 0.0243 (9) | 0.0123 (9) | -0.0007 (9) |
| S1 | 0.0288 (3) | 0.0306 (3) | 0.0257 (3) | 0.0085 (2) | 0.0063 (2) | 0.0008 (2) |
| C1 | 0.0290 (12) | 0.0316 (13) | 0.0265 (12) | 0.0036 (10) | 0.0048 (10) | 0.0033 (10) |
| C2 | 0.0251 (11) | 0.0282 (12) | 0.0260 (12) | 0.0080 (9) | 0.0044 (9) | 0.0069 (9) |
| C3 | 0.0253 (11) | 0.0268 (12) | 0.0258 (12) | 0.0086 (9) | 0.0054 (9) | 0.0055 (9) |
| C4 | 0.0259 (12) | 0.0389 (14) | 0.0329 (13) | 0.0008 (10) | 0.0040 (10) | 0.0036 (11) |
| C5 | 0.0325 (13) | 0.0565 (17) | 0.0374 (15) | 0.0052 (12) | 0.0158 (11) | 0.0127 (13) |
| C6 | 0.0401 (14) | 0.0504 (16) | 0.0287 (13) | 0.0143 (12) | 0.0131 (11) | 0.0086 (12) |
| C7 | 0.0335 (13) | 0.0382 (14) | 0.0265 (12) | 0.0087 (11) | 0.0029 (10) | 0.0021 (10) |

Geometric parameters (\AA , $^\circ$)

| | | | |
|--------------------------------------|-------------|----------|-------------|
| Cd1—O5 ⁱ | 2.2555 (18) | O6—H6B | 0.8500 |
| Cd1—O5 | 2.2555 (18) | O7—H7A | 0.8499 |
| Cd1—O4 ⁱ | 2.2589 (17) | O7—H7B | 0.8500 |
| Cd1—O4 | 2.2589 (17) | S1—C3 | 1.783 (2) |
| Cd1—O6 ⁱ | 2.2947 (18) | C1—C2 | 1.485 (3) |
| Cd1—O6 | 2.2947 (18) | C1—H1 | 0.9300 |
| N1—C1 | 1.270 (3) | C2—C7 | 1.390 (3) |
| N1—N1 ⁱⁱ | 1.431 (4) | C2—C3 | 1.403 (3) |
| O1—S1 | 1.4621 (19) | C3—C4 | 1.382 (3) |
| O2—S1 | 1.4523 (19) | C4—C5 | 1.384 (4) |
| O3—S1 | 1.4414 (18) | C4—H4 | 0.9300 |
| O4—H4A | 0.8500 | C5—C6 | 1.377 (4) |
| O4—H4B | 0.8500 | C5—H5 | 0.9300 |
| O5—H5A | 0.8500 | C6—C7 | 1.385 (4) |
| O5—H5B | 0.8500 | C6—H6 | 0.9300 |
| O6—H6A | 0.8499 | C7—H7 | 0.9300 |
| O5 ⁱ —Cd1—O5 | 180.0 | O3—S1—O1 | 111.68 (12) |
| O5 ⁱ —Cd1—O4 ⁱ | 95.45 (7) | O2—S1—O1 | 111.24 (12) |
| O5—Cd1—O4 ⁱ | 84.55 (7) | O3—S1—C3 | 106.73 (11) |
| O5 ⁱ —Cd1—O4 | 84.55 (7) | O2—S1—C3 | 106.56 (11) |
| O5—Cd1—O4 | 95.45 (7) | O1—S1—C3 | 105.47 (10) |
| O4 ⁱ —Cd1—O4 | 180.0 | N1—C1—C2 | 120.7 (2) |
| O5 ⁱ —Cd1—O6 ⁱ | 89.86 (7) | N1—C1—H1 | 119.7 |
| O5—Cd1—O6 ⁱ | 90.14 (7) | C2—C1—H1 | 119.7 |
| O4 ⁱ —Cd1—O6 ⁱ | 90.19 (7) | C7—C2—C3 | 118.4 (2) |
| O4—Cd1—O6 ⁱ | 89.81 (7) | C7—C2—C1 | 119.8 (2) |
| O5 ⁱ —Cd1—O6 | 90.14 (7) | C3—C2—C1 | 121.7 (2) |
| O5—Cd1—O6 | 89.86 (7) | C4—C3—C2 | 120.5 (2) |
| O4 ⁱ —Cd1—O6 | 89.81 (7) | C4—C3—S1 | 118.63 (17) |
| O4—Cd1—O6 | 90.19 (7) | C2—C3—S1 | 120.88 (17) |
| O6 ⁱ —Cd1—O6 | 180.0 | C3—C4—C5 | 120.0 (2) |

| | | | |
|----------------------------|--------------|-------------|--------------|
| C1—N1—N1 ⁱⁱ | 111.5 (2) | C3—C4—H4 | 120.0 |
| Cd1—O4—H4A | 113.7 | C5—C4—H4 | 120.0 |
| Cd1—O4—H4B | 123.5 | C6—C5—C4 | 120.3 (2) |
| H4A—O4—H4B | 108.3 | C6—C5—H5 | 119.9 |
| Cd1—O5—H5A | 116.0 | C4—C5—H5 | 119.9 |
| Cd1—O5—H5B | 123.2 | C5—C6—C7 | 120.0 (2) |
| H5A—O5—H5B | 108.7 | C5—C6—H6 | 120.0 |
| Cd1—O6—H6A | 116.9 | C7—C6—H6 | 120.0 |
| Cd1—O6—H6B | 123.6 | C6—C7—C2 | 120.8 (2) |
| H6A—O6—H6B | 109.5 | C6—C7—H7 | 119.6 |
| H7A—O7—H7B | 105.6 | C2—C7—H7 | 119.6 |
| O3—S1—O2 | 114.51 (12) | | |
| N1 ⁱⁱ —N1—C1—C2 | 176.2 (2) | O3—S1—C3—C2 | -47.1 (2) |
| N1—C1—C2—C7 | -29.2 (4) | O2—S1—C3—C2 | -169.90 (19) |
| N1—C1—C2—C3 | 154.3 (2) | O1—S1—C3—C2 | 71.8 (2) |
| C7—C2—C3—C4 | 0.5 (3) | C2—C3—C4—C5 | -0.7 (4) |
| C1—C2—C3—C4 | 177.1 (2) | S1—C3—C4—C5 | 177.7 (2) |
| C7—C2—C3—S1 | -177.85 (18) | C3—C4—C5—C6 | 0.3 (4) |
| C1—C2—C3—S1 | -1.2 (3) | C4—C5—C6—C7 | 0.3 (4) |
| O3—S1—C3—C4 | 134.5 (2) | C5—C6—C7—C2 | -0.5 (4) |
| O2—S1—C3—C4 | 11.7 (2) | C3—C2—C7—C6 | 0.1 (4) |
| O1—S1—C3—C4 | -106.6 (2) | C1—C2—C7—C6 | -176.6 (2) |

Symmetry codes: (i) $-x+1, -y+1, -z+1$; (ii) $-x+1, -y+1, -z$.

Hydrogen-bond geometry (\AA , $^\circ$)

| $D—\text{H}\cdots A$ | $D—\text{H}$ | $\text{H}\cdots A$ | $D\cdots A$ | $D—\text{H}\cdots A$ |
|--|--------------|--------------------|-------------|----------------------|
| O4—H4A ⁱⁱⁱ —O2 ⁱⁱⁱ | 0.85 | 1.94 | 2.783 (3) | 171 |
| O4—H4B ^{iv} —O1 ⁱ | 0.85 | 2.03 | 2.872 (2) | 174 |
| O5—H5A ^v —O1 ^{iv} | 0.85 | 1.99 | 2.831 (3) | 173 |
| O5—H5B ^v —O7 ^v | 0.85 | 2.00 | 2.843 (3) | 173 |
| O6—H6A ^{vi} —O7 | 0.85 | 2.08 | 2.881 (3) | 157 |
| O6—H6B ⁱⁱ —N1 ⁱⁱ | 0.85 | 2.15 | 2.993 (3) | 169 |
| O7—H7A ^{vii} —O3 ^{vi} | 0.85 | 1.85 | 2.692 (3) | 172 |
| O7—H7B ^{vii} —O2 ^{iv} | 0.85 | 2.21 | 3.002 (3) | 156 |

Symmetry codes: (iii) $x-1, y-1, z$; (i) $-x+1, -y+1, -z+1$; (iv) $-x+2, -y+1, -z+1$; (v) $-x+1, -y, -z+1$; (ii) $-x+1, -y+1, -z$; (vi) $x, y-1, z$.

supplementary materials

Fig. 1

